



# Document details

[Back to results](#) | 1 of 1

[Export](#) [Download](#) [Print](#) [E-mail](#) [Save to PDF](#) [Add to List](#) [More... >](#)

Kuwait Journal of Science [Open Access](#)  
Volume 45, Issue 3, 2018, Pages 14-28

## Efficient estimation in ZIP models with applications to count data (Article)

Mohamad, N.N., Mohamed, I., Kok-Haur, N., Yahya, M.S.

Institute of Mathematical Sciences, Faculty of Science, University of Malaya, Kuala Lumpur, 50603, Malaysia

### Abstract

[View references \(24\)](#)

Estimating functions have been used in estimating parameters of many continuous time series models. However, this method has not been applied to models involving count data. In this paper, we use quadratic estimating functions (QEF) to derive estimators for the joint estimation of the conditional mean and variance parameters of count data models, specifically the basic zero-inflated Poisson (ZIP) model, ZIP regression model and integer-valued generalized autoregressive heteroscedastic model with ZIP conditional distribution. Results show that the estimators derived from QEF method, which uses information from combined estimating functions, is more informative than linear estimating functions (LEF) method that only uses information from component estimating functions. Finally, we also fit the real data sets using the ZIP models via QEF, LEF and maximum likelihood methods, and in so doing, demonstrate the superiority of the QEF method in practice. © 2018 University of Kuwait. All rights reserved.

### SciVal Topic Prominence [①](#)

Topic: Random Coefficient | Autoregressive Process | Estimating Function

Prominence percentile: 34.235



### Author keywords

[Count data](#) [Information matrix](#) [Linear estimating functions](#) [Quadratic estimating functions](#) [Zero-inflated poisson](#)

### Funding details

#### Funding text

The authors wish to thank the editors and the referees for their valuable comments and suggestions. This research is financially supported by the Fundamental Research Grant Scheme (No. FP012-2013A).

**ISSN:** 23074108  
**Source Type:** Journal  
**Original language:** English

**Document Type:** Article  
**Publisher:** University of Kuwait

### References (24)

[View in search results format >](#)

All [Export](#) [Print](#) [E-mail](#) [Save to PDF](#) [Create bibliography](#)

Metrics [②](#) [View all metrics >](#)



### PlumX Metrics

Usage, Captures, Mentions,  
Social Media and Citations  
beyond Scopus.

Cited by 0 documents

Inform me when this document  
is cited in Scopus:

[Set citation alert >](#)

[Set citation feed >](#)

### Related documents

Estimating function method for  
product autoregressive models

Balakrishna, N. , Muhammed,  
P.A.

(2017) *Communications in  
Statistics: Simulation and  
Computation*

Combined estimating function  
for random coefficient models  
with correlated errors

Mohamed, I. , Khalid, K. , Yahya,  
M.S.

(2016) *Communications in  
Statistics - Theory and Methods*

Modelling the risk or price  
durations in financial markets:  
Quadratic estimating functions  
and applications

Kok-Haur, N. , Shelton, P. ,  
Thavaneswaran, A.  
(2015) *Economic Computation  
and Economic Cybernetics  
Studies and Research*

[View all related documents based  
on references](#)

Find more related documents in  
Scopus based on:

[Authors >](#) [Keywords >](#)

1

Abaza, B.A.

A recursive formulation for the two-step least squares estimator

(1982) *Journal of the University of Kuwait (Science)*, 9 (1), pp. 77-86.

---

2

Allen, D., Ng, K.H., Peiris, S.

Estimating and simulating Weibull models of risk or price durations: An application to ACD models

(2013) *North American Journal of Economics and Finance*, 25, pp. 214-225. Cited 12 times.  
doi: 10.1016/j.najef.2012.06.013

[View at Publisher](#)

---

3

Bahadur, R.R.

Examples of inconsistency of maximum likelihood estimates

(1958) *Sankhya: The Indian Journal of Statistics*, 20, pp. 207-210. Cited 24 times.

---

4

Baksh, M.F., Böhning, D., Lerdsuwansri, R.

An extension of an over-dispersion test for count data

(2011) *Computational Statistics and Data Analysis*, 55 (1), pp. 466-474. Cited 18 times.  
<http://www.elsevier.com/inca/publications/store/5/0/5/5/3/9/>  
doi: 10.1016/j.csda.2010.05.015

[View at Publisher](#)

---

5

Bera, A.K., Bilias, Y., Simlai, P.

Estimating functions and equations: An essay on historical developments with applications to econometrics  
(2006) *Palgrave Handbook of Econometrics*, 1, pp. 427-476. Cited 18 times.

---

6

Brockwell, P.J., Davis, R.A.

(1991) *Time Series: Theory and Methods*, pp. 106-110. Cited 5095 times.  
Springer Science & Business Media. New York

---

7

Chan, K.S., Ledolter, J.

Monte Carlo EM estimation for time series models involving counts

(1995) *Journal of the American Statistical Association*, 90 (429), pp. 242-252. Cited 177 times.  
doi: 10.1080/01621459.1995.10476508

[View at Publisher](#)

---

8

Chandra, S.A., Taniguchi, M.

Estimating functions for nonlinear time series models

(2001) *Annals of the Institute of Statistical Mathematics*, 53 (1), pp. 125-141. Cited 22 times.  
doi: 10.1023/A:1017924722711

[View at Publisher](#)

---

9

Crowder, M.

On linear and quadratic estimating functions

(1987) *Biometrika*, 74 (3), pp. 591-597. Cited 72 times.  
doi: 10.1093/biomet/74.3.591

[View at Publisher](#)

- 10 Godambe, V.P.  
The foundations of finite sample estimation in stochastic processes  
(1985) *Biometrika*, 72 (2), pp. 419-428. Cited 177 times.  
doi: 10.1093/biomet/72.2.419  
[View at Publisher](#)
- 
- 11 Godambe, V.P., Heyde, C.C.  
(2010) *Quasi-likelihood and Optimal Estimation*, pp. 386-399. Cited 6 times.  
Selected Works of CC Heyde, Springer. New York
- 
- 12 Kharrati-Kopaei, M., Faghih, H.  
Inferences for the inflation parameter in the zip distributions: The method of moments  
(2011) *Statistical Methodology*, 8 (4), pp. 377-388. Cited 2 times.  
doi: 10.1016/j.stamet.2011.02.005  
[View at Publisher](#)
- 
- 13 Lambert, D.  
Zero-inflated poisson regression, with an application to defects in manufacturing  
(1992) *Technometrics*, 34 (1), pp. 1-14. Cited 1925 times.  
doi: 10.1080/00401706.1992.10485228  
[View at Publisher](#)
- 
- 14 Liang, Y., Thavaneswaran, A., Abraham, B.  
Joint estimation using quadratic estimating function [\(Open Access\)](#)  
(2011) *Journal of Probability and Statistics*, art. no. 372512. Cited 10 times.  
doi: 10.1155/2011/372512  
[View at Publisher](#)
- 
- 15 Merkouris, T.  
Transform martingale estimating functions [\(Open Access\)](#)  
(2007) *Annals of Statistics*, 35 (5), pp. 1975-2000. Cited 13 times.  
[http://projecteuclid.org/DPubS/Repository/1.0/Disseminate?  
handle=euclid-aos/1194461719&view=body&content-type=pdfview\\_1](http://projecteuclid.org/DPubS/Repository/1.0/Disseminate?handle=euclid-aos/1194461719&view=body&content-type=pdfview_1)  
doi: 10.1214/009053607000000299  
[View at Publisher](#)
- 
- 16 Nanjundan, G., Naika, T.R.  
Asymptotic comparison of method of moments estimators and maximum likelihood estimators of parameters in zero-inflated poisson model  
(2012) *Applied Mathematics*, 3 (6), pp. 610-616. Cited 3 times.
- 
- 17 Kok-Haur, N., Shelton, P.  
Modelling high frequency transaction data in financial economics: A comparative study based on simulations  
(2013) *Economic Computation and Economic Cybernetics Studies and Research*, 47 (2). Cited 5 times.  
<http://www.ecocyb.ase.ro/20132/Ng%20Kok-Haur,%20Peiris,%20Shelton%28T%29.pdf>

- 18 Kok-Haur, N., Shelton, P., Thavaneswaran, A., Kooi-Huat, N.  
Modelling the risk or price durations in financial markets: Quadratic estimating functions and applications  
(2015) *Economic Computation and Economic Cybernetics Studies and Research*, 49 (1). Cited 3 times.  
<http://www.ecocyb.ase.ro/>
- 

- 19 Staub, K.E., Winkelmann, R.  
Consistent estimation of zero-inflated count models  
(2013) *Health Economics (United Kingdom)*, 22 (6), pp. 673-686. Cited 28 times.  
doi: 10.1002/hec.2844  
[View at Publisher](#)
- 

- 20 Thavaneswaran, A., Abraham, B.  
ESTIMATION FOR NON-LINEAR TIME SERIES MODELS USING ESTIMATING EQUATIONS  
(1988) *Journal of Time Series Analysis*, 9 (1), pp. 99-108. Cited 59 times.  
doi: 10.1111/j.1467-9892.1988.tb00457.x  
[View at Publisher](#)
- 

- 21 Thavaneswaran, A., Liang, Y., Frank, J.  
Inference for random coefficient volatility models  
(2012) *Statistics and Probability Letters*, 82 (12), pp. 2086-2090. Cited 6 times.  
doi: 10.1016/j.spl.2012.07.008  
[View at Publisher](#)
- 

- 22 Thavaneswaran, A., Ravishanker, N., Liang, Y.  
Generalized duration models and optimal estimation using estimating functions  
(2014) *Annals of the Institute of Statistical Mathematics*, 67 (1), pp. 129-156. Cited 8 times.  
<http://www.kluweronline.com/issn/0020-3157>  
doi: 10.1007/s10463-013-0442-9  
[View at Publisher](#)
- 

- 23 Vinod, H.  
Using godambe-durbin estimating functions in econometrics  
(1997) *Lecture Notes-Monograph Series*, pp. 215-237. Cited 9 times.  
<http://www.jstor.org/stable/4356018>
- 

- 24 Zhu, F.  
Zero-inflated Poisson and negative binomial integer-valued GARCH models  
(2012) *Journal of Statistical Planning and Inference*, 142 (4), pp. 826-839. Cited 53 times.  
doi: 10.1016/j.jspi.2011.10.002  
[View at Publisher](#)
- 

✉ Mohamed, I.; Institute of Mathematical Sciences, Faculty of Science, University of Malaya, Kuala Lumpur, Malaysia;  
email:imohamed@um.edu.my  
© Copyright 2018 Elsevier B.V., All rights reserved.

[< Back to results](#) | 1 of 1

[^ Top of page](#)

ELSEVIER

[Terms and conditions ↗](#) [Privacy policy ↗](#)

Copyright © Elsevier B.V. All rights reserved. Scopus® is a registered trademark of Elsevier B.V.

We use cookies to help provide and enhance our service and tailor content. By continuing, you agree to the use of cookies.

 RELX