

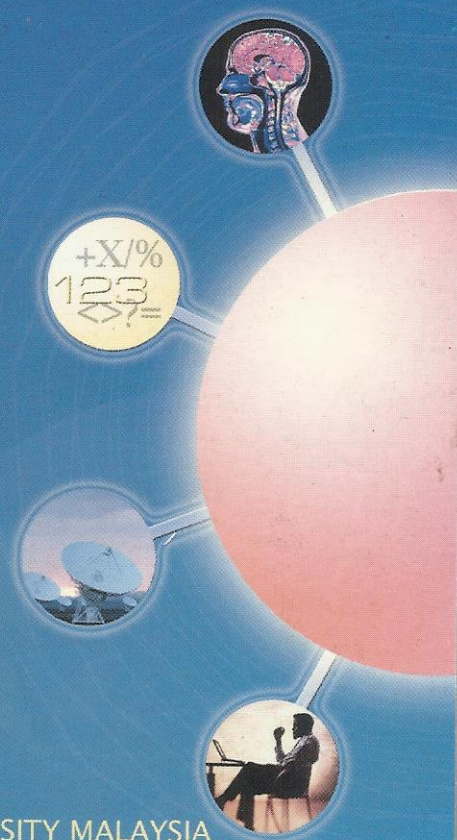
# THE ANALYTIC HIERARCHY PROCESS:

AN EFFECTIVE  
MULTI-CRITERIA  
DECISION MAKING  
TOOL

RAFIKUL ISLAM



INTERNATIONAL ISLAMIC UNIVERSITY MALAYSIA



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