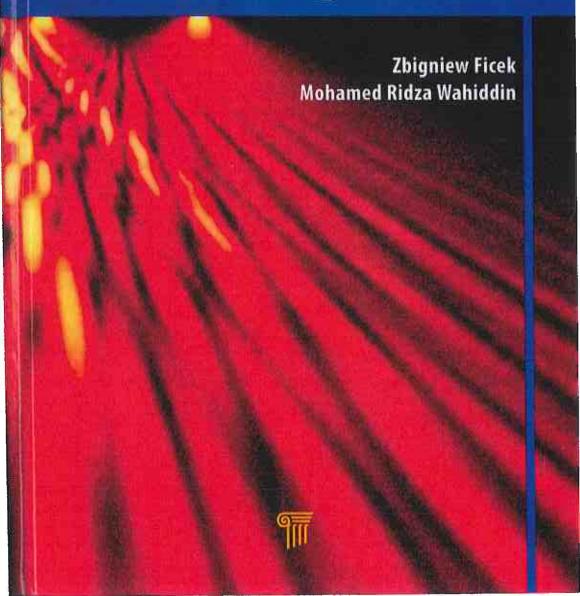
Quantum Optics for Beginners



Published by

Pan Stanford Publishing Pte. Ltd. Penthouse Level, Suntec Tower 3 8 Temasek Boulevard Singapore 038988

Email: editorial@panstanford.com Web: www.panstanford.com

British Library Cataloguing-in-Publication DataA catalogue record for this book is available from the British Library.

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ISBN 978-981-4411-75-2 (Hardcover) ISBN 978-981-4411-76-9 (eBook)

Printed in the USA

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