Mathematics Lessons Learned from Across the World
Prekindergarten-Grade 8

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NATIONAL COUNCIL OF TEACHERS OF MATHEMATICS

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Chapter 10

Making Pink-Rose Drink

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MATH CONTENT
Measurement of volume
Converting between measures
Multiply and divide compound quantities
Solve word problems
Use communication, connections, mental computation and estimation, visualization, and problem solving

MATERIALS NEEDED
Measuring cylinder
Water
Soda can filled with water
Red water (water mixed with red food coloring)
White water (water mixed with white food coloring)
Container that will hold about 2 L
Activity sheets for students
Poster paper or chart paper to record thinking and answers
Setting the Scene

Country of Context
Brunei has adopted English as the primary language of instruction. Thus, many students have to adapt to a new language while learning mathematics. Teachers of many classes in Brunei tend to be highly teacher centered, possibly as a result of students learning in a second language (Khalid 2008). However, more activities such as the one presented here allow flexibility in using groups for instruction as well as allowing more open-ended problems for class use. This activity is suitable for primary students ages eleven or older. The new Brunei Primary Mathematics Curriculum (CDD 2006) specifically mentions communication as one of the processes that need to be developed with the teaching of mathematical content.

Classroom Context
This sixty-minute activity allows for whole class instruction, group work in groups of four, and presentation time.

Teacher Notes

Task A
The first task is centered on the teacher talking to students about how to mix a drink for the class. Students then demonstrate how to measure and mix one version of the drink.

Task B
The teacher tells the entire class the following story:
Upin and Ipin are celebrating their birthday. They want to serve Opah’s special pink-rose drink. So, Upin and Ipin asked for the recipe to make the drink. Opah listed the following items needed to make a jug of the drink:

- 1000 mL water
- 250 mL rose cordial syrup (or similar other flavored syrup available locally)
- 300 mL milk
- 260 mL soda

Upin and Ipin went to the grocery store and found the following:

- 1 bottle of mineral water is sold in a 1.5-L bottle
- 1 bottle of rose cordial is sold only in 1-liter bottles
- 1 1-L bottle of milk
- 1 can of soda contains 330 mL
The teacher asks the students to work in groups to help decide how much has to be bought to make five jugs of the drink. Additionally, students are asked to record their thinking and answer on either poster paper or chart paper for sharing.

Answers may include the following:

- 4 bottles of mineral water
- 2 bottles of rose cordial
- 2 cartons of milk
- 4 cans of soda

A suggested rubric for assessing the posters and sharing the group work is given in Table 10.1.

**Table 10.1.**

**Suggested rubric for assessing posters**

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<th>Level</th>
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<td>4 Distinguished</td>
<td>Shows complete understanding of a problem's mathematical concepts and procedures&lt;br&gt;Performs algorithms completely and correctly&lt;br&gt;Always uses appropriate mathematical notation (e.g., labels answers)&lt;br&gt;Identifies all relevant information and shows complete understanding&lt;br&gt;Selects a creative and efficient strategy for solving the problem&lt;br&gt;Shows clear evidence of a complete and systematic solution process&lt;br&gt;Gives an elaborate and effective explanation of the solution process&lt;br&gt;Successfully explains &quot;solution&quot; to others&lt;br&gt;Uses precise mathematical language</td>
</tr>
<tr>
<td>3 Proficient</td>
<td>Shows near complete understanding of a problem's mathematical concepts and procedures&lt;br&gt;Performs algorithms completely; computations may contain minor errors&lt;br&gt;Often uses appropriate mathematical notation&lt;br&gt;Identifies most relevant information and shows a general understanding&lt;br&gt;Selects an appropriate strategy for solving the problem&lt;br&gt;Shows some evidence of a systematic solution process&lt;br&gt;Gives an effective explanation of the solution process&lt;br&gt;Uses appropriate mathematical language</td>
</tr>
<tr>
<td>2 Apprentice</td>
<td>Shows some understanding of a problem's mathematical concepts and procedures&lt;br&gt;Performs algorithms that may contain major computational errors&lt;br&gt;Seldom uses appropriate mathematical notation&lt;br&gt;Identifies some relevant information and shows limited understanding&lt;br&gt;Selects a strategy but unable to effectively arrive at a solution&lt;br&gt;Shows little evidence of a systematic solution process&lt;br&gt;Gives some explanation of the solution process but may be vague or difficult to interpret&lt;br&gt;Uses some mathematical language appropriately</td>
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Table 10.1. (continued)

<table>
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<tr>
<th>Level</th>
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| 1 Novice | • Shows limited or no understanding of a problem’s mathematical concepts or procedures  
• Performs algorithms that may contain major computational errors  
• Misuses or omits appropriate mathematical notation  
• Identifies little or no relevant information  
• Selects an inappropriate strategy for solving the problem  
• Shows no evidence of a systemic solution process  
• Gives minimal explanation of the solution process; may fail to explain or omits significant parts of the problem  
• Does not use mathematical language or uses it inappropriately |

Extensions

This problem may be adapted with recipes from anywhere in the world. A different problem could be created by considering buying in local markets where more exact amounts can be purchased. Then a question of how much to buy may include fractional quantities not allowed when preexisting containers must be purchased. To do this, the teacher must be very aware of local buying and selling practices.

Research Notes

Communication is a mathematical practice that seems to be necessary in today’s classrooms. Besides playing a role as an instrument for thinking mathematically, language is important for verbal representations, together with other representations such as diagrams, concrete materials, and symbols (Khalid 2008). In Brunei, some students are unwilling to speak in class as recognized by Martin (1996) when he said that apart from choral chanting, there is very little verbal output by students in Brunei classrooms. He added that when there is verbal output it is very often in the form of simple verbal recall statements. Salleh (2005) suggests that pupils in the Bruneian culture are not used to giving their views in a classroom setting. This activity is one of many now being tried to change the culture.

In the Common Core State Standards for Mathematics, the grade 4 (age 10) standards say that students should “use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit” (National Governors Association Center for Best Practices [NGA Center] and Council of Chief State School Officers [CCSSO] 2010, p. 31).

REFERENCES

Curriculum Department Darussalam (CDD), Mathematics Syllabus for Lower and Upper Primary School. Curriculum Department, Ministry of Education, Brunei Darussalam, 2006.


Activity Sheet

Task A
Read the recipe for making the pink-rose drink; decide how to make any measurement conversions needed, and be prepared to demonstrate to the class how to make the drink in the empty jug.

**Pink-Rose Drink Recipe**
Ingredients
- 1000 mL water
- 250 mL red water
- 300 mL white water
- 260 mL soda

_Supplies provided by teacher:
- 1.5 L bottle of water
- 1 L red water
- 1 L white water
- 1 can of soda water
- 1 empty jug_

Task B
Upin and Ipin are celebrating their birthday. They want to serve Opah’s special pink-rose drink. So, Upin and Ipin asked for the recipe to make the drink. Opah listed the following items needed to make a jug of the drink:
- 1000 mL water
- 250 mL rose cordial syrup (or similar other flavored syrup available locally)
- 300 mL milk
- 260 mL soda
Activity Sheet

Upin and Ipin went to the grocery store and found the following:

- 1 bottle of mineral water is sold in a 1.5-L bottle
- 1 bottle of rose cordial is sold only in 1-liter bottles
- 1 1-liter bottle of milk
- 1 can of soda contains 330 mL

Decide how much has to be bought to make 5 jugs of the drink.

Record your thinking and answers on either poster paper or chart paper for sharing.