

WAVELET ANALYSIS

**CONCEPTS AND APPLICATIONS
IN IMAGE PROCESSING**

OTHMAN OMRAN KHALIFA



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Concepts and Applications in Image Processing

Othman Omran Khalifa



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