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NINE

AIRCRAFT EQUATIONS OF MOTION

A non linear model

9.1. Introduction

In this chapter, the orientation and position of the aircraft motion based on the non-linear model is described before developing the aircraft equation of motion. The equation is first derived in the form of Euler’s force and moment equations of motions. The full equations of motion include also the effect of spinning rotors.

9.2. Orientation and Position of the Airplane

The position and orientation of the airplane are given relative to the Earth-fixed frame $F_E$. The CG has position vector $r_c$, with coordinates $(x_E, y_E, z_E)$.

The orientation of the airplane is given by a series of three consecutive rotations known as the Euler angles. The airplane is imagined first to be oriented such that its axes are parallel to those of $F_E$, hence its position is $C x_1 y_1 z_1$. Then the following rotations are applied:

1. A rotation $\psi$ about $o z_1$, carrying the axes to $C x_2 y_2 z_2$.
2. A rotation $\theta$ about $o y_2$, carrying the axes to $C x_3 y_3 z_3$
3. A rotation $\phi$ about $o x_3$ carrying the axes to $C x_4 y_4 z_4$

where the ranges are limited to

$$-\pi \leq \psi < \pi \text{ or } 0 \leq \psi \leq 2\pi$$

$$-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

$$-\pi \leq \phi < \pi \text{ or } 0 \leq \phi \leq 2\pi$$  \hspace{1cm} (9.1)

In a vertical climb or dive,