Nasir Ganikhodjaev Farrukh Mukhamedov Pah Chin Hee

VOLUME 1

x' = 2xy y' = 2xz

INVESTIGATIONS ON PURE MATHEMATICS, FINANCE MATHEMATICS AND OPTICS

Proceedings of the Department of Computational and Theoretical Sciences Kulliyyah of Science, IIUM

 $w_1(x, y, z) = z$ $w_2(x, y, z) = z$

 $z' = x^2 + y^2 + z^2 + 2yz$

 $w_1 N_1 w_1 = N_{17}$



Investigations on Pure Mathematics, Finance Mathematics and Optics

Nasir Ganikhodjaev Farrukh Mukhamedov Pah Chin Hee



Published by. IIUM Press International Islamic University Malaysia

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Perpustakaan Negara Malaysia

Cataloguing-in-Publication Data

Nasır Ganikhodjaev, Farrukh Mukhamedov & Pah Chin Hee Investigations on Pure Mathematics, Finance Mathematics and Optics

ISBN: 978-967-418-198-7

Member of Majlıs Penerbitan İlmiah Malaysıa – MAPIM (Malaysıan Scholarly Publishing Council)

Printed by
IIUM PRINTING SDN.BHD.
No 1, Jalan Industri Batu Caves 1/3
Taman Perindustrian Batu Caves
Batu Caves Centre Point
68100 Batu Caves
Selangor Darul Ehsan

Contents

Preface

Part I Pure Mathematics Concentration

Chapter 1	THE BEHAVIOR OF TRAJECTORY OF ξ ^s QUADRATIC STOCHASTIC OPERATIONS	•
		2
Chapter 2	THEORY OF MARKOV CHAINS IN PEDIATRIC DISEASES	8
Chapter 3	ON NONLINEAR DYNAMIC SYSTEMS ARISING IN POTTS MODEL	14
Chapter 4	THE FIRST RETURN TIME AND DIMENSION	22
Chapter 5	ON AS SOCIATIVE ALGEBRAIC STRUCTURE OF GENETIC INHERITANCE	31
Chapter 6	INTERACTING PARTICLE SYSTEM	37
Chapter 7	DYNAMICS OF GENERALIZED LOGISTIC MAPS	43
Chapter 8	GEOMETRIC BROWNIAN MOTION AND CALCULATION OF OPTION PREMIUM IN BLACK SCHOLES MODEL	50
Chapter 9	ON THE ELEMENTARY CHARACTEFIZATION OF PRIMES IN PRIMALITY TESTS: TWO SHORT STUDIES.	57
Chapter 10	ON ASSOCIATIVE ALGEBRAIC STRTJCTURE OF GENETIC INHERITANCE	64
Chapter 11	SOME APPLICATION OF ERGODIC THEORY IN NUMBER THEORY	70
Chapter 12	STUDY OF ROLES OF EXTERNAL MAGNETIC FIELD ON ISING AND POTTS MODEL	76
Chapter 13	INVESTIGATION OF STABILITY OF FIXED POINTS OF NONLINEAR DISCRETE DYNAMICAL SYSTEMS	82
Chapter 14	MARKOV CHAINS AND ITS APPLICATION: THE INVENTORY MODEL	90
Chapter 15	PHASE TRANSITION FOR ISING MODEL WITH TWO COMPETING INTERACTION ON CAYLEY TREE OF ORDER 4	96
Chapter 16	LIMIT BEHAVIOR OF DYNAMIC SYSTEMS CORRESPONDING TO LATTICE MODELS WITH COMPETING PROLONGED AND ONE-LEVEL BINARY INTERACTIONS	101
Chapter 17	ASSOCIATIVE ALGEBRA IN GENETIC INHERITANCE	109
Chapter 18	ON ξ ^a - QUADRATIC STOCHASTIC OPERATORS AND THEIR CLASSIFICATIONS	115

Part II Finance Mathematics Concentration

Chapter 19	ANALYZING THE PERFORMANCE OF INVESTMENT STRATEGY OF EPF	123
Chapter 20	PREDICTION OF STOCK PRICE USING NEURAL NETWORK	130
Chapter 21	COMPARISON BETWEEN CONVENTIONAL AND ISLAMIC BOND IN MALAYSIA	136
Chapter 22	STOCK PERFORMANCE ANALYSIS BETWEEN MALAYSIAN AIRLINES SYSTEM BERHAD AND AIRASIA BERHAD	144
Chapter 23	ISLAMIC PAWNBROKING (AR-RAHNU) AS A MICRO CREDIT INSTRUMENT IN MALAYSIA	151
Chapter 24	ANALYSIS OF CRUDE PALM OIL FUTURES PRICES TRADED ON BURSA MALAYSIA	160
Chapter 25	AN EMPIRICAL STUDY ON THE EFFICIENCY OF THE TRIM AND FILL METHOD IN CORRECTING PUBLICATION BIAS IN META ANALYSIS	166
Chapter 26	PERFORMANCE ANALYSIS OF INSURANCE AND TAKAFUL INDUSTRIES IN MALAYSIA	171
Chapter 27	ANALYSIS OF DATA USING MULTILEVEL MODELLING WITH MLwiN	179
Chapter 28	FINANCIAL PERFORMANCE OF' ISLAMIC BANKING AND CONVENTIONAL BANKING IN MALAYSIA	186
Chapter 29	A STUDY ON THE EFFECT OF PUBLICATION BIAS IN META ANALYSIS	194
Chapter 30	RATIO ANALYSIS: BANK ISLAM MALAYSIA BERHAD (BIMB) & MALAYAN BANKING BERHAD (MAYBANK)	201
Chapter 31	AN ANALYSIS OF MALAYSIAN UNIT TRUST FUNDS: ISLAMIC VS CONVENTIONAL	207
	Part III Optics Concentration	
Chapter 32	QUANTUM TRAJECTORY METHOD USING MPI PARALLEL COMPUTING	214
Chapter 33	LINEAR WAVE PROPAGATION IN SINGLE MODE OPTICAL FIBRE	220
Chapter 34	THE OPTICAL RAY TRACING TECHNIQUE IN LENS SYSTEM WITHIN AND BEYOND PARAXIAL APPROXIMATION	226
Chapter 35	WAVE PROPAGATION IN NONLINEAR AND HOMOGENEOUS MEDIAKERR MEDIA	234
Chapter 36	MATRIX METHODS OF OPTICAL RESONATORS	240

GEOMETRIC BROWNIAN MOTION AND CALCULATION OF OPTION PREMIUM IN BLACK SCHOLES MODEL

Izzati Mat Assist. Prof. Dr. Pah Chin Hee

Abstract. This project paper examines the simplest of all random motion of the stochastic process which well known as Brownian motion. The motion is used to construct Geometric Brownian motion that lead to the introduction of Black Scholes Model. Black Scholes model gives the market player standard way to price an option. Then, the simulations of the Brownian motion and Geometric Brownian motion using Maple are presented. One of the assumptions of Black Scholes Model is the behavior of the price of underlying asset following Geometric Brownian motion will be tested. Finally, the formula is used to find the price of the Gold Option for both put and call type of option using the data of Kijang Emas gold price.

1 Introduction of Single Brownian Motion Path

Step 1: Let BM is a function of n where n is number of points to be considered.

Step 2: Set X, W, A, c as local variables. Then, use Statistics and ListTools packages. Statistics used to create X which is a RandomVariable function whereas ListTools used for the PartialSums function for W.

Step 3: Define

X: Random variable which has normal distribution with mean 0 and standard deviation of $\frac{1}{\sqrt{n}}$ where $\frac{1}{n}$ is the step size.

W: A trajectory which is a partial sums of i (i is the sequence taken from a sample of X) start with 0.

$$W_t = W_{t-1} + i$$
 $t = 0, 1, ..., n$

c: A sequence of $\frac{j}{n}$, where j = 0, 1, ..., n

Step 4: Print W with c as x-coordinate using BM(n) function

