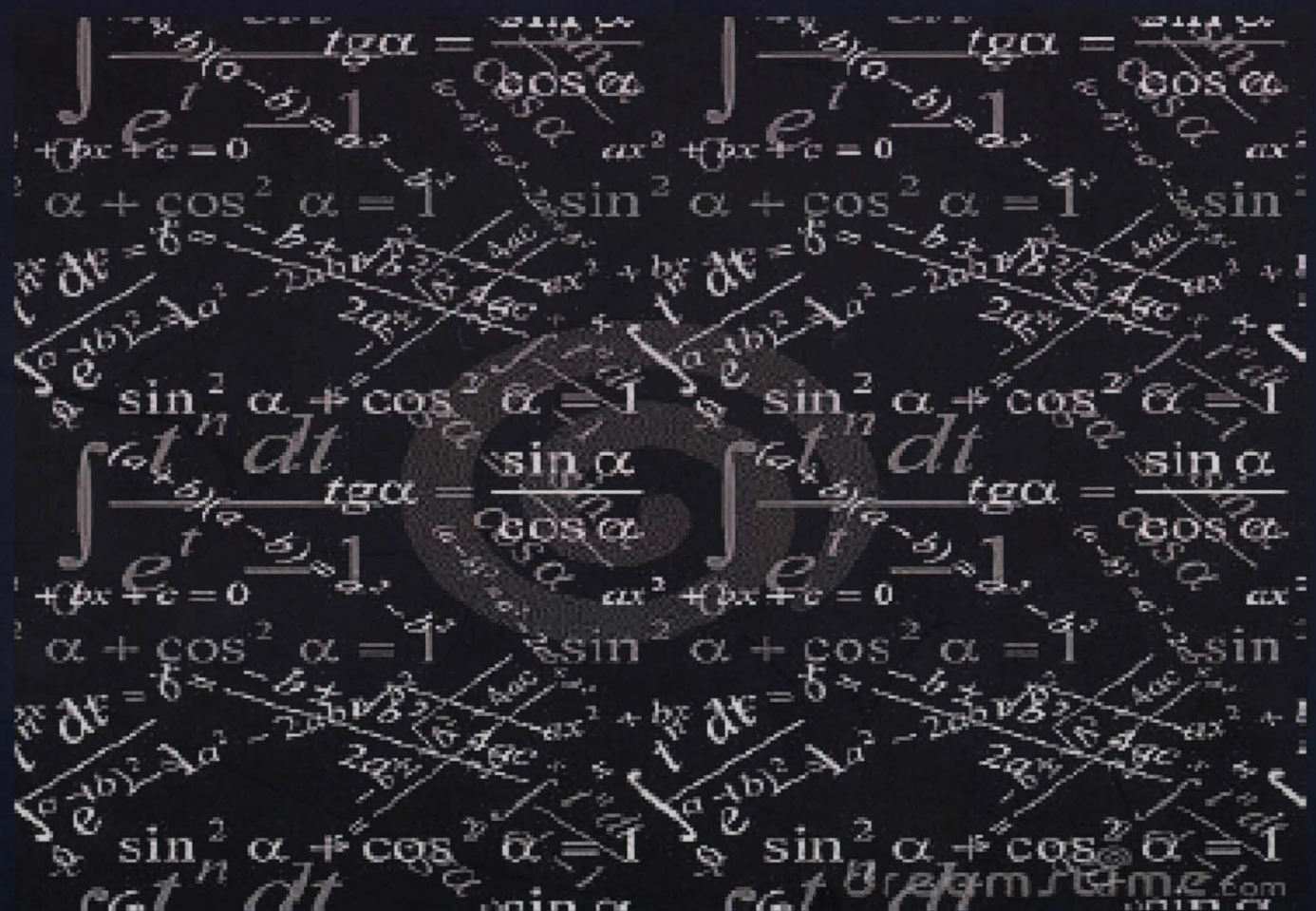




# RECENT ACHIEVEMENTS IN DYNAMICAL SYSTEMS

Proceedings of Department of  
Computational and Theoretical  
Sciences, Faculty of Science, IIUM



Chief Editor : Farrukh Mukhamedov

Editors : Nasir Ganikhodjaev

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## Contents

### Part I. Quadratic Operators and Their Dynamics

Farrukh Mukhamedov, Abduaziz Abduganiev, Maksut Mukhamedov, On Dynamics of a Class of Quantum Quadratic Operators on $M_2(\mathbb{C})$ .	2
Mansoor Saburov, On Ergodic Principle for Quadratic Volterra Operators.	9
Mansoor Saburov, Fixed Point of Compositions of Volterra Operators.	15
Farrukh Mukhamedov, Afifah Hanum Bt Mohd. Jamal, Classification of $\xi^s$ - Quadratic Stochastic Operators in 2D-Simplex.	21
Farrukh Mukhamedov, Mansoor Saburov, Afifah Hanum Bt Mohd. Jamal, Dynamics of $\xi^s$ - Quadratic Stochastic Operators in 2D-Simplex.	29
Farrukh Mukhamedov, Mansoor Saburov, Some Examples of Lotka-Volterra Type Models.	34
Nasir Ganikhodjaev, Makhsuma Usmanova, On Linearization of Quadratic Stochastic Operators.	40
Nasir Ganikhodjaev, Continual Family of Ergodic Non-Homogeneous Markov Chains.	47
Rasul Ganikhodjaev, Farrukh Mukhamedov, Mansoor Saburov, On G-Decomposition of Matrices.	53
Farrukh Mukhamedov, On $L_1$ -Weak Ergodicity of Nonhomogeneous Discrete Markov Processes	59
Inomjon Ganiev, Farrukh Mukhamedov, On Measurable Bundles of $C^*$ -Dynamical Systems.	65
Inomjon Ganiev, Farrukh Mukhamedov, A Weighted Ergodic Theorem for Contractions Defined on Banach-Kantorovich Lattice.	71

## **Part II. Dynamical Systems Arising From Physical Models**

Farrukh Mukhamedov, Mansoor Saburov, Dynamical Systems of XY-Models On A Cayley Tree Of Order Two.	78
Farrukh Mukhamedov, Mansoor Saburov, Dynamical Systems of XY-Models On A Cayley Tree Of Order Three.	85
Farrukh Mukhamedov, Mansoor Saburov, Dynamical Systems of Ising Model on a Cayley Tree.	91
Nasir Ganikhodjaev, Siti Fatimah Zakaria, Phase Diagram of The Ising Model with Nearest-Neighbor Interactions.	98
Nasir Ganikhodjaev, Siti Fatimah Zakaria, Ising Model on a General Cayley Tree with Competing Next-Nearest-Neighbour Interactions.	107
Pah Chin Hee, Rukiah Ali, Ising Model with Competing Interactions on Cayley Tree of Order Four	118
Massimo Ostilli, Langevin Dynamics for a New Class of Mean-Field Ising Models.	125
Farrukh Mukhamedov, Utkir Rozikov, Free Energy of The Ising Model with Competing Interactions on a Cayley Tree.	133
A. Benseghir, B.A. Umarov, A. Messikh, Modulational Instability In Salerno Model.	141
Nasir Ganikhodjaev, Seyit Temir, On Potts Model with Triple Interactions.	146
Nasir Ganikhodjaev, Ashraf Mohamed Nawi, Mohd Hirzie Mohd Rodzhan, Phase Diagram Of The Potts Model with External Magnetic Field.	152
Nasir Ganikhodjaev, Fatimah Abdul Razak, A Correlation Inequality for Potts Model.	160
Nasir Ganikhodjaev, Ashraf Mohamed Nawi, A Nonlinear Dynamic System Arising in Potts Model.	167

Farrukh Mukhamedov, On Existence of Phase Transition for One Dimensional P-Adic Countable State Potts Model.	177
B.A. Umarov, A. Bouketir, Strongly Localized Models In Two-Component Discrete Media With Cubic-Quintic Nonlinearity.	184
<b>Part III. Nonlinear Dynamical Systems</b>	
Farrukh Mukhamedov , Wan Nur Fairuz Alwani Wan Rozali, On P-Adic Generalized Logistic Dynamical System.	196
Farrukh Mukhamedov, Mansoor Saburov, On Equation $x^q = a$ over $\mathcal{Q}_p$ .	201
Farrukh Mukhamedov, Mansoor Saburov, On Unification of The Strong Convergence Theorems for a Finite Family Of TAN Mappings in Banach Spaces.	207
<b>Part IV. Graphs And Networks</b>	
Pah Chin Hee, Single Polygon Counting for Two Fixed Nodes on a Cayley Tree of Order 2.	214
Khikmat Saburov, Mansoor Saburov, Every 3-Connected $K_{1,3}Z_6$ -Free Graph is Hamiltonian.	219
Khikmat Saburov, Mansoor Saburov, Relation Between $K_{1,3}P_7$ -Free and $K_{1,3}N_{1,1,1}$ -Free Graphs.	224
Khikmat Saburov, Mansoor Saburov, Hamiltonicity Of $K_{1,3}B_{i,7-i}$ -Free Graphs.	232
Saadi Bin Ahmad Kamtuddin , Nor Azura Md Ghani, Choong-Yeun Liong And Abdul Aziz Jemain, Artificial Neural Network Implementation on Firearm Recognition System via Ring Firing Pin Impression Image.	242
Pah Chin Hee, Dirichlet's Theorem And Prime Gap Statistics.	256

# DIRICHLET'S THEOREM AND PRIME GAP STATISTICS

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## Abstract

In this paper, we suggest an investigation on a special prime gap problem which associate directly to Dirichlet's theorem and connect it to twin prime conjecture.

**Keywords:** *Prime number; Dirichlet's Theorem; statistics.*

## Introduction

Dirichlet's theorem [1] stated that there are infinite many prime in any arithmetic progression  $an + b$ , for any fixed  $a, b$ , while Ben-Green theorem [2] stated that there are arbitrary long arithmetic progression in primes. In both theorems, the notion of prime gap is implicitly used but the actual study of prime gaps is focus on two consecutive primes. The common problem for prime gaps is the first occurrence of large gaps [3, 4, 5] and frequency distribution of prime gaps [6]. If the frequency of gap with distance 2 is a non-zero measure, then this implies twin primes conjecture.

In this paper, we suggest an investigation on a special prime gap problem which associate directly to Dirichlet's theorem and connect it to twin prime conjecture. It is obvious that each pair of twin prime will take the form of  $(6k + 5, 6k + 7)$ . According to Dirichlet's theorem, integer taking the form either  $6k+5$  or  $6k+1$  has infinitely many primes, there are also infinitely many pair of consecutive prime in the form of  $(6k_1 + 5, 6k_2 + 1)$ . Therefore we would like to ask the converse: given a pair of consecutive primes  $(6k_1 + 5, 6k_2 + 1)$ , how many of them are twin primes?

## Basic Setting

Let  $P$  denotes the sequences of prime numbers  $\{2, 3, 5, 7, \dots\}$  and

$D = \{(x, y) \in P^2 \mid x \text{ and } y \text{ are consecutive primes that } x = 6k_1 + 5 \text{ and } y = 6k_2 + 1 > x\}$

. From this set we define each class- $i$  by the subset of  $D$ , i.e.

$$D_i = \{(x, y) \in D \mid y - x = i\}.$$