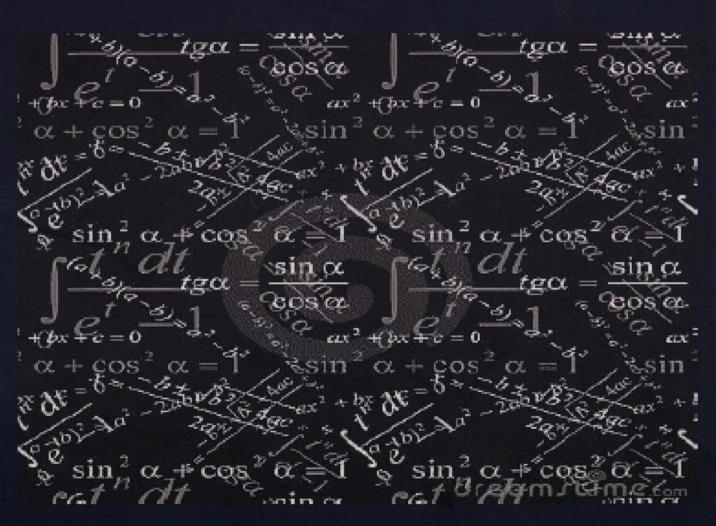
**VOLUME 2** 

# RECENT ACHIEVEMENTS IN DYNAMICAL SYSTEMS

Proceedings of Department of Computational and Theoretical Sciences, Faculty of Science, IIUM



Chief Editor: Farrukh Mukhamedov

Editors : Nasir Ganikhodjaev

: Mansoor Saburov

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Vol. 2



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### CONTINUAL FAMILY OF ERGODIC NON-HOMOGENEOUS MARKOV CHAINS

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#### Abstract

Inspired by the recent work of Jiahong Shen on a geometric approach to ergodic non-homogeneous Markov chains, we construct a continual family of ergodic non-homogeneous Markov chains on finite states.

#### **Quadratic Stochastic Operator**

Let

$$S^{m-1} = \{ \mathbf{x} = (x_1, \dots, x_m) \in R^m : x_i \ge 0, \sum_{i=1}^m x_i = 1 \}$$

is the (m-1) -dimensional canonical simplex in  $\mathbb{R}^m$ . The transformation  $V: \mathbb{S}^{m-1} \to \mathbb{S}^{m-1}$  is called a quadratic stochastic operator(q.s.o.) if

$$V: (V\mathbf{x})_k = \sum_{i,j=1}^m p_{ij,k} x_i x_j, \quad (k = 1, \dots, m)$$
 (1)

where

$$a)p_{ij,k} \ge 0; \quad b)p_{ij,k} = p_{ji,k}; \quad \text{and} \quad c)\sum_{k=1}^{m} p_{ij,k} = 1$$

for arbitrary  $i, j, k = 1, \dots, m$ . Quadratic stochastic operator was first introduced in [1]. Such operator frequently arises in many models of mathematical genetics [1-3]. Consider a biological population, that is a community of organisms closed with respect to reproduction. Assume that each individual in this population belongs to precisely one species  $1, \dots, m$ . The scale of species is such that the species of the parents i and j unambiguously determines the probability of every species k for the first generation of direct descendants. Denote this probability, that is to be called the heredity coefficient, by  $p_{ii,k}$ . It is then obvious that  $p_{ii,k} \ge 0$  for all i,j,k and that

$$\sum_{k=1}^{m} p_{ij,k} = I(i,j,k=1,\cdots,m).$$