FIRST EDITION

$$\int \frac{f'(x)}{f(x)}\,dx = \ln|f(x)| + C$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

PRε$^{C\alpha LCULUS}_{\sum_{k=2}^{10}(2k-1)}$

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PRE CALCULUS

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