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Alp, M.[a] , Pah, C.H.[b] , Saburov, M.K.[a]

The description of generalized translation-invariant p-adic Gibbs measures for the Potts model on the Cayley tree of order three
(2023) *Theoretical and Mathematical Physics(Russian Federation)*, 214 (3), pp. 406-420.

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Abstract
Abstract: We describe generalized translation-invariant p-adic Gibbs measures for the Potts model on the Cayley tree of order three, confirming and extending the related results in the literature. We introduce a cube root function over the p-adic field Q_p, which enables us to explicitly prescribe all roots of the cubic monomial equation over Q_p. © 2023, Pleiades Publishing, Ltd.

Author Keywords
Cayley tree; Gibbs measure; p-adic field; Potts model

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